

# Analysis and Design of RCC and Post-tensioned Flat Slabs Considering Seismic Effect

Boskey Vishal Bahoria and Dhananjay K. Parbat

**Abstract**—The post-tensioning method is now a days increasing widely, due to its application. By using post-tensioning method one can design the most economic and the safe design. While using this method more precautions has to be made for shear and deflection criteria for the slabs. The design of post-tensioned flat slab can be done by using load balancing and equivalent frame method. For the application of design procedure an office building is considered as a case study. The plan of the office building (G+4) is considered. This building is designed by considering four cases with different floor systems. The quantities of reinforcing steel, prestressing steel, concrete required for the slab, beam and column is calculated for the same and are presented in tabular form. Along with this total cost of the building per square meter is found and comparison of all the four cases with respect to cost is done.

**Index Terms**—Equivalent frame method, flat slab, load balancing method, post-tensioned, RCC, seismic analysis, strud, staad-pro.

## I. INTRODUCTION

As the floor system plays an important role in the overall cost of a building, a post-tensioned floor system is invented which reduces the time for the construction and finally the cost of the structure. In some countries, including the U.S., Australia, South Africa, Thailand and India, a great number of large buildings have been successfully constructed using post-tensioned floors. The reason for this lies in its decisive technical and economical advantages. According to Park.E.H.Kim *et al* [1] and Y. H. Luo, A. Durrani [2] the most important advantages offered by post-tensioning systems are as follows -

- By comparison with reinforced concrete, a considerable saving in concrete and steel since, due to the working of the entire concrete cross-section more slender designs are possible.
- Smaller deflections compared to with steel and reinforced concrete structures.
- Good crack behavior and therefore permanent protection of the steel against corrosion.
- Almost unchanged serviceability even after considerable overload, since temporary cracks close again after the overload has disappeared.
- High fatigue strength, since the amplitude of the stress changes in the prestressing steel under alternating loads are quite small.

- If a significant part of the load is resisted by post-tensioning the non-prestressed reinforcement can be simplified and standardized to a large degree. Furthermore, material handling is reduced since the total tonnage of steel (non-prestressed + prestressed) and concrete is less than for a Reinforced Concrete floor.
- Assembling of precast elements by post-tensioning avoids complicated reinforcing bar connections with insitu closure pours, or welded steel connectors, and thus can significantly reduce erection time.
- Usually the permanent floor load is largely balanced by draped post-tensioning tendons so that only the weight of the wet concrete of the floor above induces flexural stresses. These are often of the same order as the design live load stresses. Post-tensioning usually balances most of the permanent loads thus significantly reducing deflections and tensile stresses.
- The P/A stress provided by post-tensioning may prevent tensile stresses causing the floor to crack.

For the above reasons post-tensioned construction has also come to be used in many situations in buildings. In addition to the above mentioned general features of post-tensioned construction systems, the following advantages of post-tensioned slabs over reinforced concrete slabs are listed as follows:

- More economical structures resulting from the use of prestressing steels with a very high tensile strength instead of normal reinforcing steels.
- Larger spans and greater slenderness, which results in reduced dead load, which also has a beneficial effect upon the columns and foundations and reduces the overall height of buildings or enables additional floors to be incorporated in buildings of a given height.

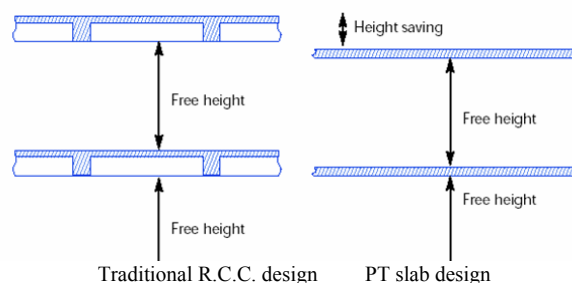


Fig. 1. Height comparison of R.C.C. & PT slab design

## II. SCOPE OF THE PRESENT STUDY

The post-tensioning method is now a days increasing widely, due to its application. By using the post-tensioning method one can design the most economic and the safe design. But while using this method more precautions has to

Manuscript received October 15, 2012; revised December 25, 2012.  
B. V. Bahoria is with Rajiv Gandhi College of Engineering and Research, Nagpur, India (e-mail: boskey\_bahoria@yahoo.co.in).  
D. K. Parbat is with Government Polytechnic, Sakoli, Dist Bhandara, India. (e-mail: parbatdk@gmail.com).

be made for the shear and the deflection criteria for the slabs. The design of the post-tension flat slab can be done by using load balancing and equivalent frame method. Among of both the equivalent frame method is widely used. In the load balancing method the 65 to 80% of the dead load is carried by the tendon itself. So that there is an upward deflection due to tendon profile resulting the reduction in overall deflection. In the present study the design of the post-tensioned flat slab is done by using both methods, load balancing method and equivalent frame method. As the shear and deflection check is the most important for the post-tensioned slabs the detail design for the shear and deflections (short term deflection and long term deflections due to creep and shrinkage) is carried out. The parametric study of the post-tensioned flat slab by varying the span by 0.5m interval is done and results of the different parameters such as thickness of slab, grade of concrete, loss due to stress, normal reinforcement, reinforcement for the shear, number of tendons, stressing force per tendon and deflection etc. are presented in the graphical form. Continuing to this a design of post-tensioned beam is also done. For the study of post-tensioned slab and beams a case study of a multistory office building (G+4) is taken and it is designed by four cases, the post-tensioned flat slab, post-tensioned beams and the R.C.C. slab, only R.C.C. flat slab and the R.C.C. slab and beams. After the design of these four cases the comparative study with respect to the economy is carried out.

### III. DESIGN METHODOLOGY

The design of post-tensioned slab is done by two methods, load balancing method and the equivalent frame method. The load balancing method introduced by T. Y. Lin is most suitable for the indeterminate structures rather than the determinate structures. In this method the 65 to 80% of dead load is balanced by the tendons so that the flexural member will not be subjected to bending stress under a given load conditions. On the other hand the equivalent frame method is widely use for the design of post-tensioned slabs. Here load balancing method and equivalent frame method are discussed in the following section.

#### A. Load-Balancing Method

The concept of load balancing is introduced for prestressed concrete structures, as per T.Y Lin *et al* [3] a third approach after the elastic stress and the ultimate strength method of design and analysis. It is first applied to simple beams and cantilevers and then to continuous beams and rigid frames. This load-balancing method represents the simplest approach to prestressed design and analysis, its advantage over the elastic stress and ultimate strength methods is not significant for statically determinate structures. When dealing with statically indeterminate systems including flat slabs and certain thin shells, load-balancing method offers tremendous advantage both in calculating and visualizing. According to load-balancing method, prestressing balances a certain portion of the gravity loads so that flexural members, such as slabs, beams, and girders, will not be subjected to bending stresses under a given load condition. Thus a structure carrying transverse loads is subjected only to axial stresses.

#### B. Equivalent Frame Method of Analysis

The equivalent frame method of analysis is known as the beam method. This method of analysis utilizes the conventional elastic analysis assumption and models the slab or slab and columns, as a beam or as a frame, respectively. This is the most widely used and applied method of analysis for the post-tensioned flat plates.

According to Y. H. Luo, A. Durrani *et al* [4] the effect of vertical of lateral services and design loading on post-tensioned flat plates, bonded or unbonded, may be analyzed as for rigid frames in accordance with the provisions of the code (IS, ACI etc.). When the columns are relatively slender or not rigidly connected to the slab, their stiffness may be neglected and continuous beam analysis applied. As per A.C. Scordelis, Lin, T.Y, and R Itaya *et al* [5] the moment induced by prestressing may also be determined by a similar analysis of a rigid frame or continuous beam, using equivalent load or load balancing concept. However it should be kept in mind that the distribution of moments due to loads may differ considerably from the distribution of moments due to prestressing. Service loads produce very pronounced moments peaks at columns, whereas the moment curve produced by post-tensioning has a more gentle undulating variation of the same form as the tendon profile.

According to A .Pan, and J. P. Moehle [6] the effects of reversed tendon curvature at supports are generally neglected in applying the load balancing method to design of flat plates since the reverse curvature has only a minor influence on the elastic moments (in the order of 5 to 10 percent), and does not affect the ultimate moment capacity. It is necessary to consider reverse tendon curvature tort adequately evaluate the shear carried by the tendons inside the critical section.

### IV. PARAMETRIC STUDY

For the purpose of parametric study of post-tensioned slab the slabs with and without drop varying from 7m to 12m at an interval of 0.5m are considered.

Load considered-Dead load –self weight

Live load – 2 KN/m<sup>2</sup>

Superimposed dead load - 1 KN/m<sup>2</sup>

Analysis and design is done by using following methods

Load balancing method

Equivalent frame method

For the application of design procedure a office building is consider as a case study. The plan of the office building (G+4) is considered. This building is designed by considering four cases with different floor systems. The different floor systems used for these four cases are as follows.

For the above four cases the quantities of reinforcing steel, prestressing steel, concrete required for the slab, beam and column is calculated and are presented in the tabular form. Along with this a total cost of the building per square meter is found and the comparison of all the four cases with respect to cost is given here.

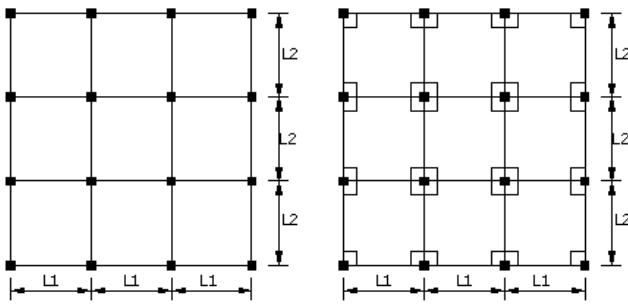


Fig. 2. Plan of slab with drop and without drop

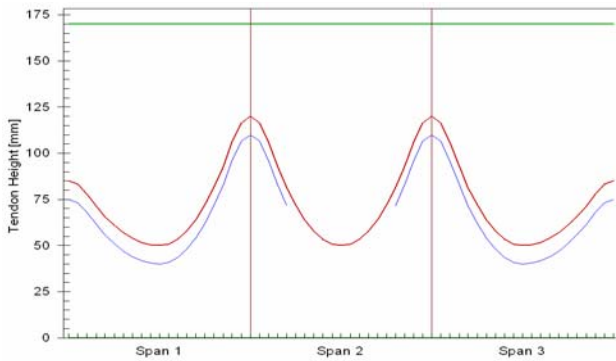


Fig. 3. Tendon profile for the slab without drop

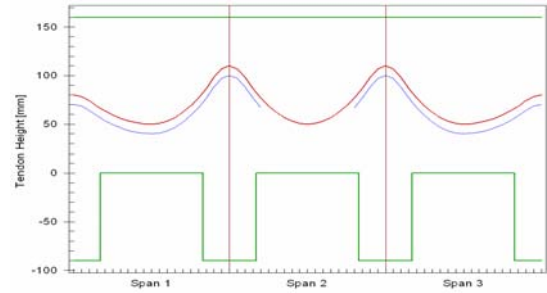


Fig. 4. Tendon profile for the slab with drop

## V. ESTIMATING AND COSTING

From the analysis and design results of the office building the total estimation for the quantities for a typical floor is calculated. The quantities of concrete, reinforcing steel, prestressing steel and the formwork and their cost according to the current rate excluding the labour charges for all the four cases are given in the table I. The rate per square meter for a typical floor (which includes slab, beam and column) of a building in each case is according to the values calculated from the detail estimation.

(Rate of concrete=4400/-per m<sup>3</sup>, Rate of steel=50/-per kg, Rate of form work=400), Rate of prestressing steel=130/-per kg)

TABLE I: RATE ANALYSIS FOR THE CASES CONSIDERED

Item	Concrete (m <sup>3</sup> )	Reinforcing steel (Kg)	Prestressing steel (Kg)	Form work	Rate per sqm
PT flat slab	507.52	31659	8400	2100	Rs. 2800/-
RC flat slab	549.69	85550	-----	2100	Rs. 3600/-
PT slab with RCC beam	641.33	42271	6720	2100	Rs. 3200/-
RCC slab with RCC beam	626.31	86701	-----	2100	Rs. 3800/-

## VI. RESULTS AND CONCLUSION

The analysis, design and the estimation of the office building for the four different floor systems is done and finally the rate per square meter for the construction of this building is found out. The fig .6 shows the variation of the rate per square meter for these four different cases.

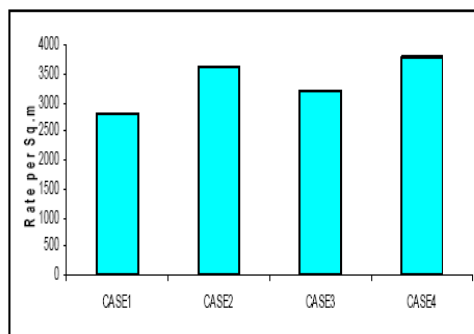


Fig. 5. Variation of rate for each floor system

The design and the estimation of the office building for the four different floor systems is done and finally the rate per square meter for the construction of this building is found out. The Fig. 6 shows the variation of the rate per square meter for these four different cases. The observation made from the above work is as follows:

- 1) From the economic point of view the post-tensioned flat slab is the most economical among all four floor systems and the reinforced concrete slab with reinforced concrete beam is the costlier one for this span.
- 2) If we consider the post-tensioned flat slab and reinforced concrete flat slab, the thickness of reinforced concrete flat slab is 12.5% greater and its cost is 27% greater than the post-tensioned flat slab.
- 3) From both post-tensioned floor system building the post-tensioned flat slab is more economical than the post-tensioned slab with reinforced concrete beams.
- 4) The quantity of prestressing steel is 4 Kg/m<sup>2</sup> for post-tensioned flat slab and 3.2 Kg/m<sup>2</sup> for post-tensioned slab with reinforced concrete beams i.e. the prestressing steel required for the post-tensioned flat slab is greater.
- 5) The reinforcing steel required for the post-tensioned flat slab and post-tensioned slab with reinforced concrete beam is 15 Kg/m<sup>2</sup> and 20.15 Kg/m<sup>2</sup> respectively.
- 6) The reinforcing steel is more in case of post-tensioned slab with reinforced concrete beams because the slab transfers the load on the beam and more loads is taken by the beams itself.
- 7) The reinforcing steel for the reinforced concrete flat slab is 41 Kg/m<sup>2</sup> while for the reinforced concrete slab and beam it is 40 Kg/m<sup>2</sup>.
- 8) The amount of concrete required for a floor is more in

case of post-tensioned slab with reinforced concrete beams while it is least for the post-tensioned flat slab floor system.

- 9) The floor to floor height available in case of post-tensioned flat and reinforced concrete flat slab is 2.65m while in case of post-tensioned slab with reinforced concrete beams and reinforced concrete slab and beams is 2.4m.
- 10) If we consider the period of construction for a floor it is less in case of post-tensioned flat slab than the other three cases as the post-tensioning allows the earlier removal of the formwork. In case of post-tensioned slab with reinforced concrete beams the formwork of slab can be removed earlier but the formwork for the reinforced concrete beams cannot be removed earlier.
- 11) While estimating the cost of the each building the labour charges are not considered, as the time period reduce the labour charges will reduce in case of post-tensioned flat slab.
- 12) The wall load is considered on all over the floor ( $\text{KN/m}^2$ ) for the post-tensioned building While analysis. So there is flexibility to the user to construct a wall wherever required in case of post-tensioning.

## VII. SEISMIC ANALYSIS

According to A. J. Duran, S.T Mau, A.A Abouhashish [7] and Y. H Luo, A. Durrani, J. Conte [ 8] the Equivalent frame method for flat slab underestimates the negative moment and overestimate positive moments. A comparative study of pt and RCC flat plate is done considering the earthquake load using Equivalent frame method in accordance to [9],[10] and using struds software the conclusions drawn are as follows:

- 1) The moment calculated for Post-tensioned flat plate slab is less as compare to moment calculated for RCC flat plate slab by equivalent frame method because as depth of Post tensioned flat plate slab 30 to 35% less than RCC plate slab, due to which self weight of slab get reduced.
- 2) Due to post-tensioning of flat plate slab there is no much effect on axial force but shear and moment on column increases.
- 3) The deflection at center of flat plate slab is controlled more effectively by parabolic and Trapezoidal tendon than triangular tendon.

- 4) Modeling flat plate slab with diaphragm and without diaphragm in case of response spectrum there is no variation in axial force, shear force and moment as moment of inertia of slab is very high it acts as rigid.
- 5) Post-tensioned design of flat plate slab allows nearly 70% reduction in steel and 30 % reduction in concrete as compared to Reinforced cement concrete flat plate slab.

## REFERENCES

- [1] E. H. K. Park, "RC Flat Plate under Combined in-Plane & Out-Of-Plane Loads," *Journal of Structural Engineering*, vol. 125, no. 10, October, 1999.
- [2] Y. H. Luo and A. Durrani, "Equivalent Beam Model for Flat-Slab Buildings: Interior Connections," *ACI Structural Journal*, vol. 92, no.1, pp. 115-124, 1995.
- [3] T. Y. Lin, "Load balancing for design and analysis of prestressed concrete structures," *Journal of American Concrete Institute*, vol. 60, no. 6, June 1963.
- [4] Y. H. Luo and A. Durrani, "Equivalent Beam Model for Flat-Slab Buildings: Exterior Connections," *ACI Structural Journal*, vol. 92, no. 2, pp. 250-257, 1995.
- [5] A. C. Scordelis, T. Y Lin, and R. Itaya , " Behavior of continuous slab prestressed in both direction," *Journal of American Concrete Institute*, vol. 40, no.3, December 1959.
- [6] A .Pan and J. P.Moehle, "Lateral Displacement Ductility of R/C Flat Plates," *ACI Structural Journal*, vol. 86, no. 3, pp. 250-258, 1989.
- [7] A. J. Duran, S. T. Mau and A. A. Abouhashish, "Earthquake response of flat-slab buildings," *Journal of Structural Engineering*, vol. 120, no.3, March, 1994.
- [8] Y. H. Luo, A. Durrani, and J. Conte, "Seismic Reliability Assessment of Existing R/C Flatslab Buildings," *Journal of Structural Engineering*, ASCE, vol.121, no.10, pp. 1522-1530, 1995.
- [9] *Code of Practice for Prestressed Concrete Is: 1343 – 1980*, BIS, Indian Standard Institution, New Delhi.
- [10] *Plain and Reinforced Concrete Code of Practice Is: 456 - 2000*, BIS, Indian Standard Institution, New Delhi.



**Boskey Vishal Bahoria** was born and brought up at Nagpur, India. D.O.B 20<sup>TH</sup> Sept.1980 She has done Masters in Structural Engineering from Nagpur University, India in 2008. Having bachelors degree(2005) Nagpur university and Diploma in civil Engineering (2002)MSBTE, Pune, India. She is persuing PHD from RTMNU, Nagpur University, and date of registration 15<sup>th</sup> Jan'2011. She is currently working as an Asst. Prof. in Civil Engineering Department, Rajiv Gandhi College of Engineering & Research, Nagpu, India. She is having 5 years teaching experience (UG). The area of research is Concrete, replacement of natural sand by quarry dust in concrete.